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# Applications of Diffusion Models

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**DMQA Open Seminar (2023. 11. 24)**

Data Mining & Quality Analytics Lab.

**박태남**

# 발표자 소개



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- Data Mining & Quality Analytics Lab. (김성범 교수님)
- M.S. Student (2023.03 ~ Present)

## ❖ Research Interest

- Deep Generative Models
- Diffusion Models

## ❖ Contact

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- Generative Models
- Diffusion Models

## ❖ Applications of Diffusion Models

- Text-to-Image Generation
- Anomaly Detection
- Natural Language Generation
- Time-series Forecasting & Imputation

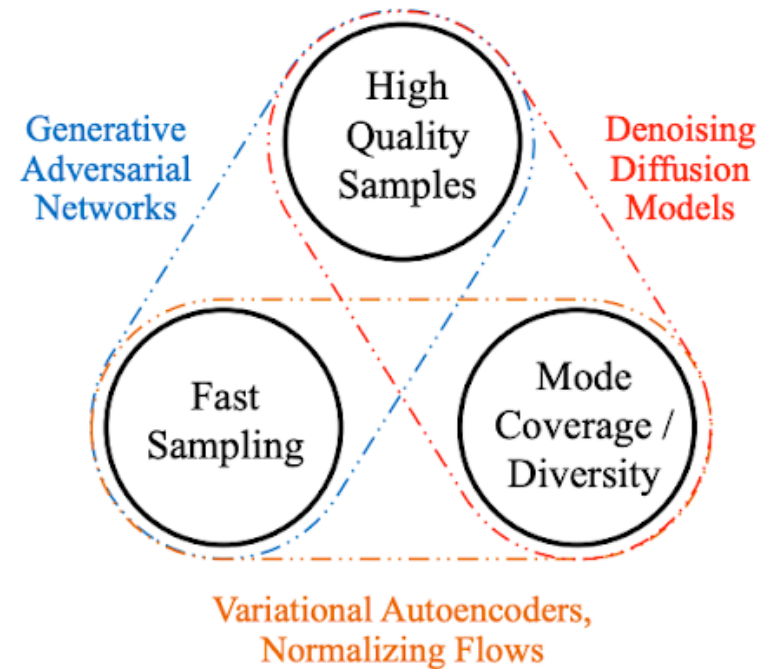
## ❖ Conclusion

# Introduction

## Generative Models

### ❖ Generative Models

- 학습된 데이터의 표현을 학습하고 데이터 자체를 모델링  $p(x)$
- 중요 요인들
  - ✓ High Quality Samples
  - ✓ Mode Coverage/Diversity
  - ✓ Fast Sampling



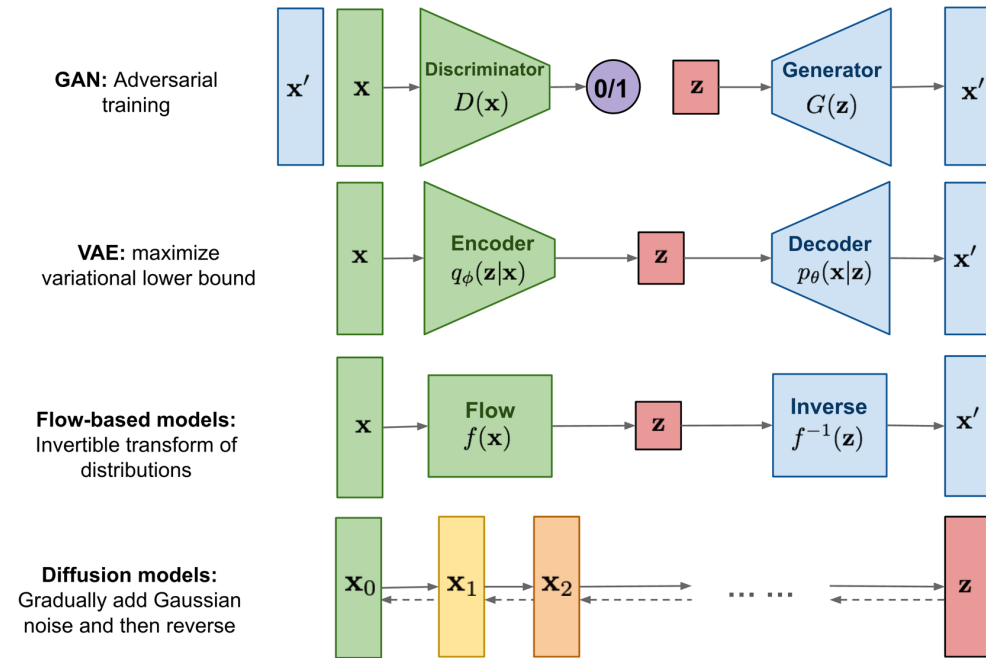
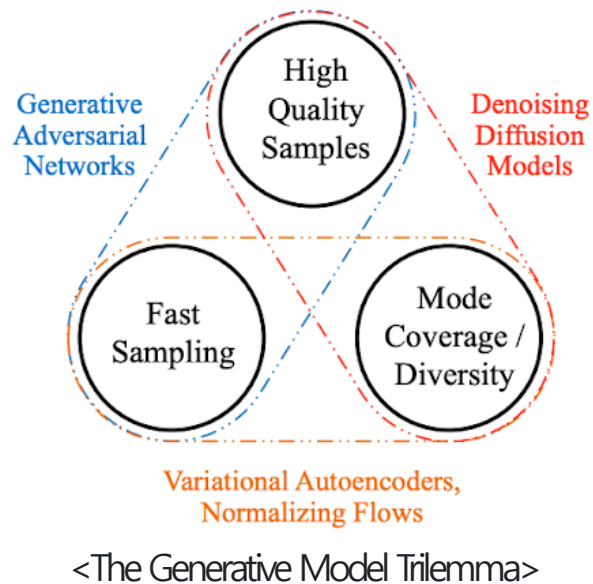
<Generative learning trilemma>

# Introduction

## Generative Models

### ❖ Generative Models $p(x)$

- **Generative Adversarial Networks(GAN):** 학습의 불안정성
- **Variational Autoencoders(VAE):** 직접 Likelihood를 최대화하지 못함
- **Flow-based models:** 역함수가 존재하는 구조에서만 사용가능



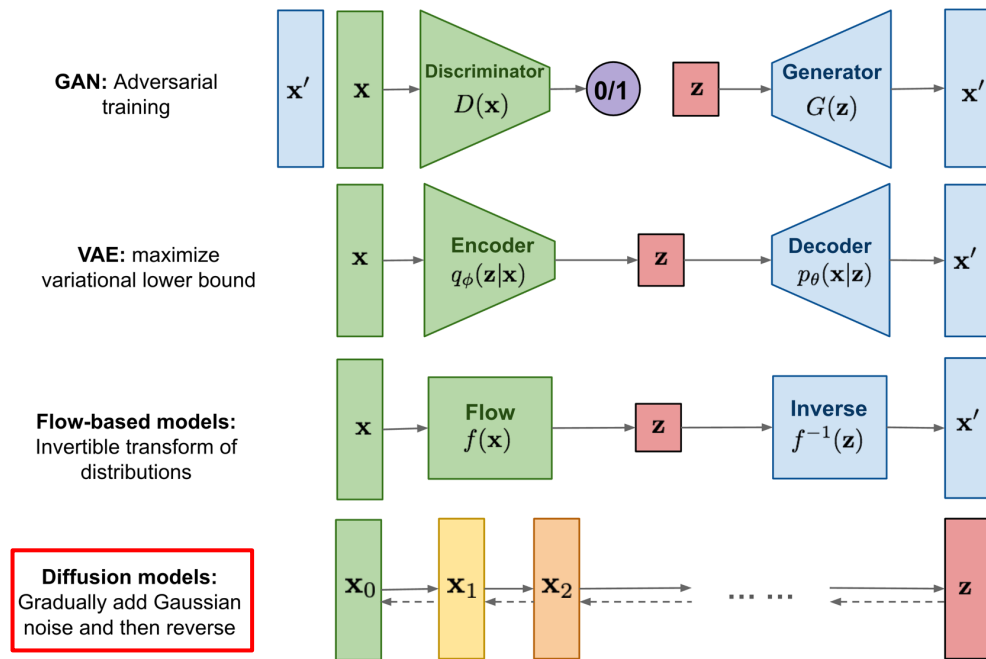
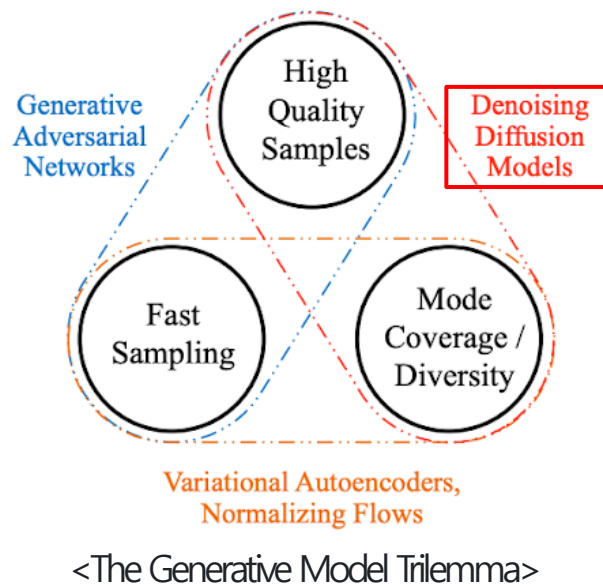
<GAN, VAE, Flow-based models, Diffusion models>

# Introduction

## Diffusion Models

### ❖ Diffusion Models

- 비정형 열역학(Non-equilibrium Thermodynamics)에 기초
- 고정된 절차로 학습되며, 잠재 변수의 차원은 원본 데이터와 동일
- High Quality Samples & Mode Coverage/Diversity



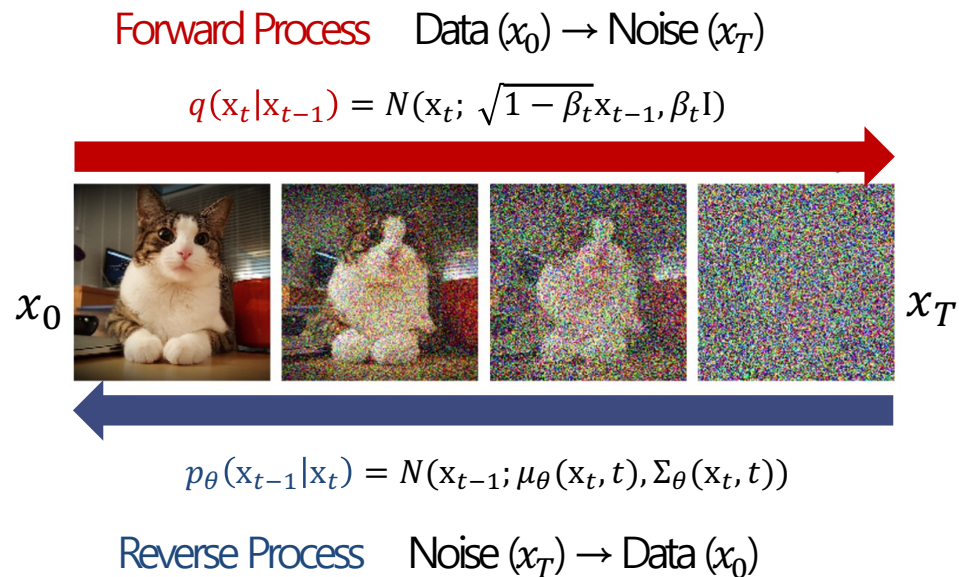
<GAN, VAE, Flow-based models, Diffusion models>

# Introduction

## Diffusion Models

### ❖ DDPM (Denoising Diffusion Probabilistic Models, 2020)

- **Forward Process:** Data ( $x_0$ )  $\rightarrow$  Noise ( $x_T$ )
- **Reverse Process:** Noise ( $x_T$ )  $\rightarrow$  Data ( $x_0$ )



### Algorithm 1 Training

- 1: **repeat**
- 2:  $\mathbf{x}_0 \sim q(\mathbf{x}_0)$
- 3:  $t \sim \text{Uniform}(\{1, \dots, T\})$
- 4:  $\epsilon \sim \mathcal{N}(\mathbf{0}, \mathbf{I})$
- 5: Take gradient descent step on  
$$\nabla_\theta \|\epsilon - \epsilon_\theta(\sqrt{\bar{\alpha}_t}\mathbf{x}_0 + \sqrt{1 - \bar{\alpha}_t}\epsilon, t)\|^2$$
- 6: **until** converged

### Algorithm 2 Sampling

- 1:  $\mathbf{x}_T \sim \mathcal{N}(\mathbf{0}, \mathbf{I})$
- 2: **for**  $t = T, \dots, 1$  **do**
- 3:  $\mathbf{z} \sim \mathcal{N}(\mathbf{0}, \mathbf{I})$  if  $t > 1$ , else  $\mathbf{z} = \mathbf{0}$
- 4:  $\mathbf{x}_{t-1} = \frac{1}{\sqrt{\alpha_t}} \left( \mathbf{x}_t - \frac{1 - \alpha_t}{\sqrt{1 - \alpha_t}} \epsilon_\theta(\mathbf{x}_t, t) \right) + \sigma_t \mathbf{z}$
- 5: **end for**
- 6: **return**  $\mathbf{x}_0$

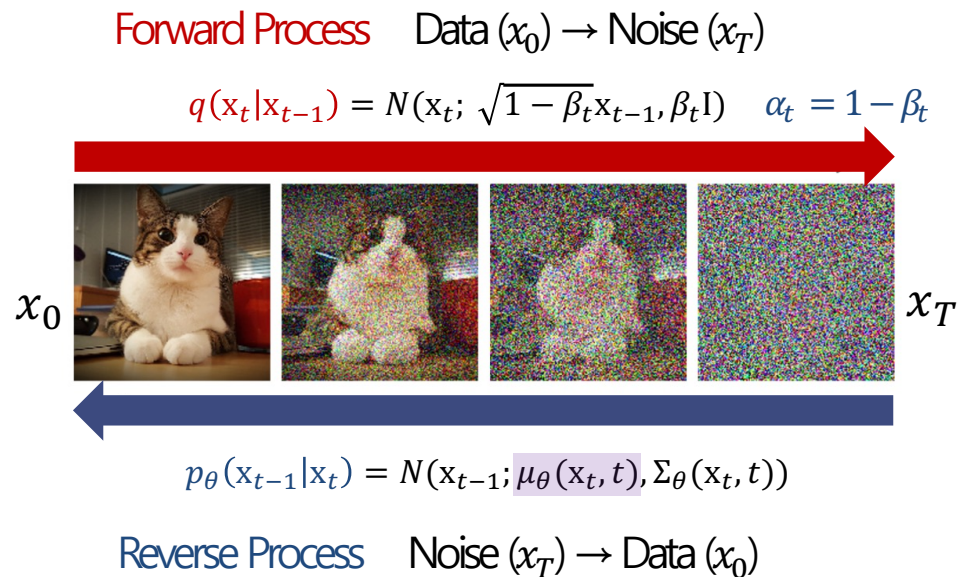
<학습 및 샘플링 과정>

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- 1: **repeat**
- 2:  $\mathbf{x}_0 \sim q(\mathbf{x}_0)$
- 3:  $t \sim \text{Uniform}(\{1, \dots, T\})$
- 4:  $\epsilon \sim \mathcal{N}(\mathbf{0}, \mathbf{I})$
- 5: Take gradient descent step on  $q(x_t|x_0) = N(x_t; \sqrt{\alpha_t}x_0, (1 - \alpha_t)\mathbf{I})$   
 $\rightarrow x_t = \sqrt{\alpha_t}x_0 + \sqrt{1 - \alpha_t}\epsilon$   
 $\nabla_\theta \|\epsilon - \epsilon_\theta(\sqrt{\alpha_t}\mathbf{x}_0 + \sqrt{1 - \alpha_t}\epsilon, t)\|^2$
- 6: **until** converged  $\epsilon_\theta(x_t, t)$

### Algorithm 2 Sampling Inference

- 1:  $\mathbf{x}_T \sim \mathcal{N}(\mathbf{0}, \mathbf{I})$
- 2: **for**  $t = T, \dots, 1$  **do**
- 3:  $\mathbf{z} \sim \mathcal{N}(\mathbf{0}, \mathbf{I})$  if  $t > 1$ , else  $\mathbf{z} = \mathbf{0}$
- 4:  $\mathbf{x}_{t-1} = \frac{1}{\sqrt{\alpha_t}} \left( \mathbf{x}_t - \frac{1 - \alpha_t}{\sqrt{1 - \alpha_t}} \epsilon_\theta(\mathbf{x}_t, t) \right) + \sigma_t \mathbf{z}$
- 5: **end for**
- 6: **return**  $\mathbf{x}_0$

<학습 및 샘플링 과정>



# Introduction

## Diffusion Models

### ❖ Conditional Diffusion Models $p(x|y)$

- **Classifier guidance**: Noisy data로 학습한 별도의 classifier의 gradients을 통해 conditional sampling
- **Classifier-free guidance (CFG)**: Diffusion Models만으로 conditional sampling 가능

w: Guidance scale

$$\hat{\epsilon}(x_t, t) = \epsilon_\theta(x_t, t) - \sqrt{1 - \bar{\alpha}_t} w \nabla_{x_t} \log f_\phi(y|x_t)$$

<Classifier guidance>

w: Guidance scale

$$\begin{aligned}\hat{\epsilon}(x_t, t, y) &= (1 + w)\epsilon_\theta(x_t, t, y) - w\epsilon_\theta(x_t, t) \\ &= w(\epsilon_\theta(x_t, t, y) - \epsilon_\theta(x_t, t)) + \epsilon_\theta(x_t, t, y)\end{aligned}$$

<Classifier-free guidance>

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## Diffusion Models

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<Classifier-free guidance>

# Introduction

## Diffusion Models

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$$\hat{\epsilon}(x_t, t) = \epsilon_\theta(x_t, t) - \sqrt{1 - \bar{\alpha}_t} w \nabla_{x_t} \log f_\phi(y|x_t)$$

<Classifier guidance>

w: Guidance scale

$$\epsilon_\theta(x_t, t) = \epsilon_\theta(x_t, t, y = \emptyset)$$

$$\begin{aligned}\hat{\epsilon}(x_t, t, y) &= (1 + w) \epsilon_\theta(x_t, t, y) - w \epsilon_\theta(x_t, t) \\ &= w (\epsilon_\theta(x_t, t, y) - \epsilon_\theta(x_t, t)) + \epsilon_\theta(x_t, t, y)\end{aligned}$$

<Classifier-free guidance>

# Introduction

## Diffusion Models

**종료** Diffusion Probabilistic Models (DDPM)

- Forward process: 데이터( $x_0$ ) + 노이즈  $\rightarrow$  랜덤 노이즈( $x_T$ )
- Reverse process: 랜덤 노이즈 ( $x_T$ ) + 노이즈 제거  $\rightarrow$  데이터( $x_0$ )
- 노이즈를 제거하는 reverse process를 학습할 수 있다면 랜덤 노이즈로부터 데이터 생성 가능

**Score-based Generative Models and Diffusion Models**

발표자: 조한샘

📅 2022년 2월 11일  
🕒 오후 1시 ~  
▶ 온라인 비디오 시청 (YouTube)

[세미나 정보 보기 →](#)

**종료** Improving Sampling Speed of Diffusion Models

Open DMQA Seminar  
2023.02.10

Jong Hyun Lee  
2023.06.09

**Conditional Diffusion Models**

발표자: 조한샘

📅 2023년 2월 10일  
🕒 오후 1시 ~  
▶ 온라인 비디오 시청 (YouTube)

[세미나 정보 보기 →](#)

**종료** Conditional Diffusion Models

Jong Hyun Lee  
2023.06.09

**Conditional Diffusion Models**

발표자: 이종현

📅 2023년 6월 16일  
🕒 오전 12시 ~  
▶ 온라인 비디오 시청 (YouTube)

[세미나 정보 보기 →](#)

**종료** Image Editing with Diffusion Model

2023. 08. 25.  
이진우  
DMQA Open Seminar

Geonhui Jang  
2023.09.15

**Image Editing with Diffusion Model**

발표자: 이진우

📅 2023년 8월 25일  
🕒 오전 12시 ~  
▶ 온라인 비디오 시청 (YouTube)

[세미나 정보 보기 →](#)

**종료** Introduction to Personalization with Diffusion Models

Geonhui Jang  
2023.09.15

**Introduction to Personalization with Diffusion Models**

발표자: 장건희

📅 2023년 9월 15일  
🕒 오후 12시 ~  
▶ 온라인 비디오 시청 (YouTube)

[세미나 정보 보기 →](#)

# Diffusion Models for Text-to-Image Generation

"GLIDE: Towards Photorealistic Image Generation and Editing with Text-Guided Diffusion Models", ICML, 2022

## ❖ Guided Language to Image Diffusion for Generation and Editing

- Text-conditional image synthesis



"a hedgehog using a calculator"



"a corgi wearing a red bowtie and a purple party hat"



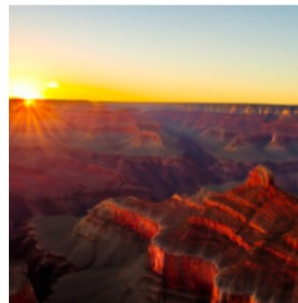
"robots meditating in a vipassana retreat"



"a fall landscape with a small cottage next to a lake"



"a surrealist dream-like oil painting by salvador dali of a cat playing checkers"



"a professional photo of a sunset behind the grand canyon"



"a high-quality oil painting of a psychedelic hamster dragon"



"an illustration of albert einstein wearing a superhero costume"

# Diffusion Models for Text-to-Image Generation

"GLIDE: Towards Photorealistic Image Generation and Editing with Text-Guided Diffusion Models", ICML, 2022

## ❖ GLIDE – Guidance

- Classifier guidance

$$\hat{\epsilon}(x_t, t) = \epsilon_\theta(x_t, t) - \sqrt{1 - \bar{\alpha}_t} w \nabla_{x_t} \log f_\phi(y|x_t)$$

- Classifier-free guidance(CFG)

$$\hat{\epsilon}(x_t, t, y) = (1 + w)\epsilon_\theta(x_t, t, y) - w\epsilon_\theta(x_t, t)$$

- CLIP Guidance

$$\hat{\epsilon}(x_t, t) = \epsilon_\theta(x_t, t) - \sqrt{1 - \bar{\alpha}_t} \nabla_{x_t} (f(x_t) \cdot g(y))$$

# Diffusion Models for Text-to-Image Generation

"GLIDE: Towards Photorealistic Image Generation and Editing with Text-Guided Diffusion Models", ICML, 2022

## ❖ GLIDE – Guidance

- Classifier guidance

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- Classifier-free guidance(CFG)

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- CLIP Guidance

$$\hat{\epsilon}(x_t, t) = \epsilon_\theta(x_t, t) - \sqrt{1 - \bar{\alpha}_t} \nabla_{x_t} (f(x_t) \cdot g(y))$$

Image encoder  
caption encoder

# Diffusion Models for Text-to-Image Generation

"GLIDE: Towards Photorealistic Image Generation and Editing with Text-Guided Diffusion Models", ICML, 2022

## ❖ Experiments

- 텍스트의 넓은 다양성을 일반화하는 능력 존재
- 고화질의 질감을 표현한 이미지 생성
- 다양한 스타일의 이미지 생성
- 여러가지 컨셉을 동시에 부여 가능



"a hedgehog using a calculator"



"a corgi wearing a red bowtie and a purple party hat"



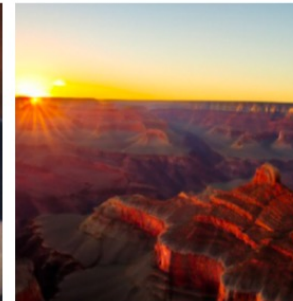
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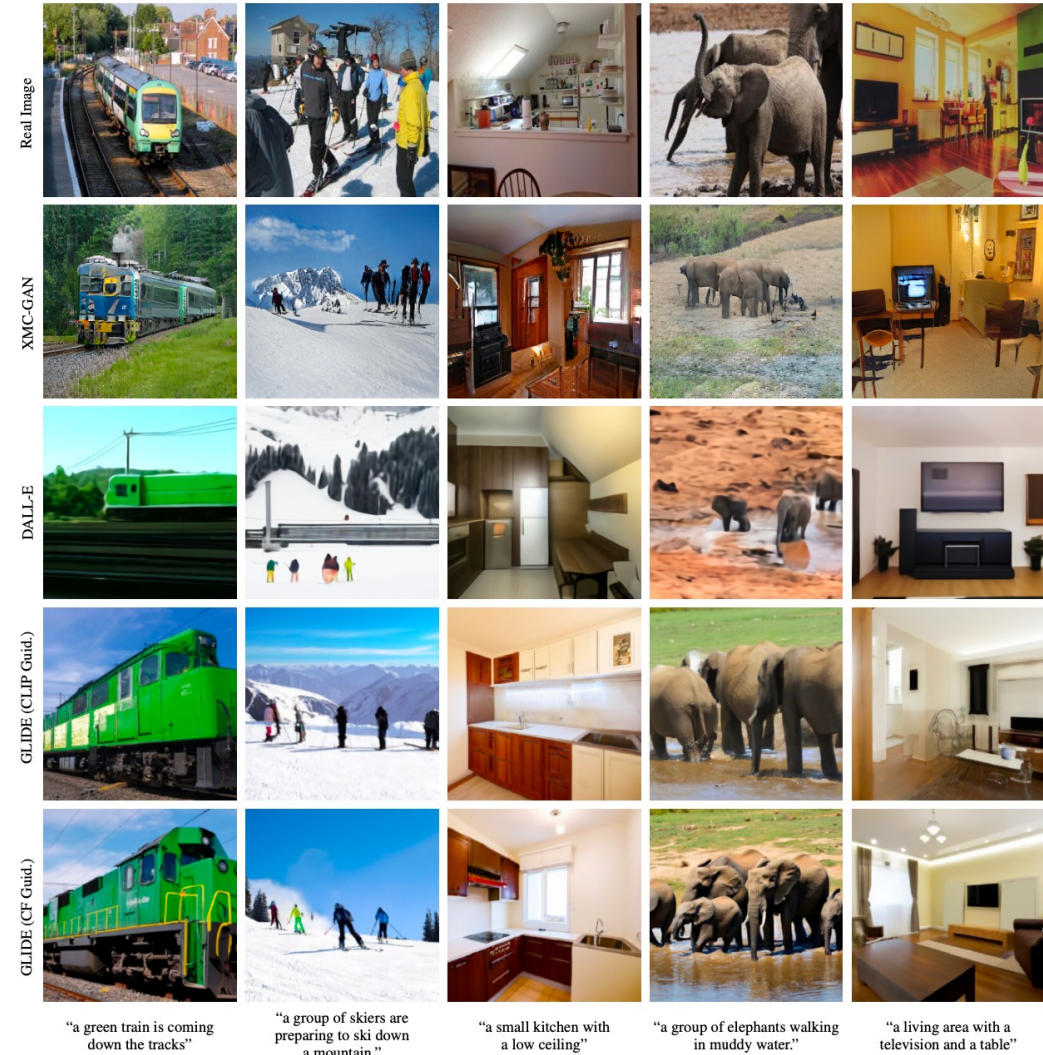


# Diffusion Models for Text-to-Image Generation

"GLIDE: Towards Photorealistic Image Generation and Editing with Text-Guided Diffusion Models", ICML, 2022

## ❖ Experiments

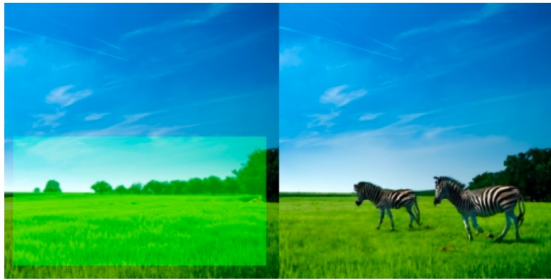
- 기존 SOTA 방법론들 대비 가장 현실적인 이미지 생성
- CLIP guidance보다 CFG가 더 현실적인 이미지 생성



# Diffusion Models for Text-to-Image Generation

"GLIDE: Towards Photorealistic Image Generation and Editing with Text-Guided Diffusion Models", ICML, 2022

## ❖ Experiments - Image inpainting & Image editing



"zebras roaming in the field"



"a girl hugging a corgi on a pedestal"



"an old car in a snowy forest"



"a man wearing a white hat"

<Text-conditional image inpainting examples>



"a corgi wearing a bow tie and a birthday hat"



"a fire in the background"



"only one cloud in the sky today"

<Text-conditional SDEdit examples>



# Diffusion Models for Text-to-Image Generation

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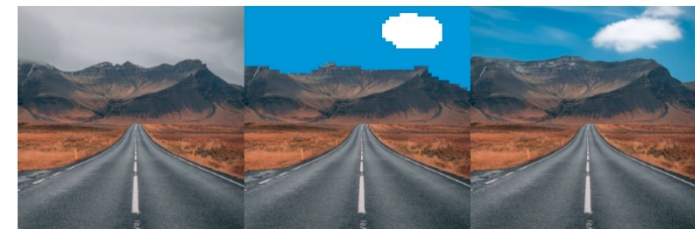
<Text-conditional image inpainting examples>



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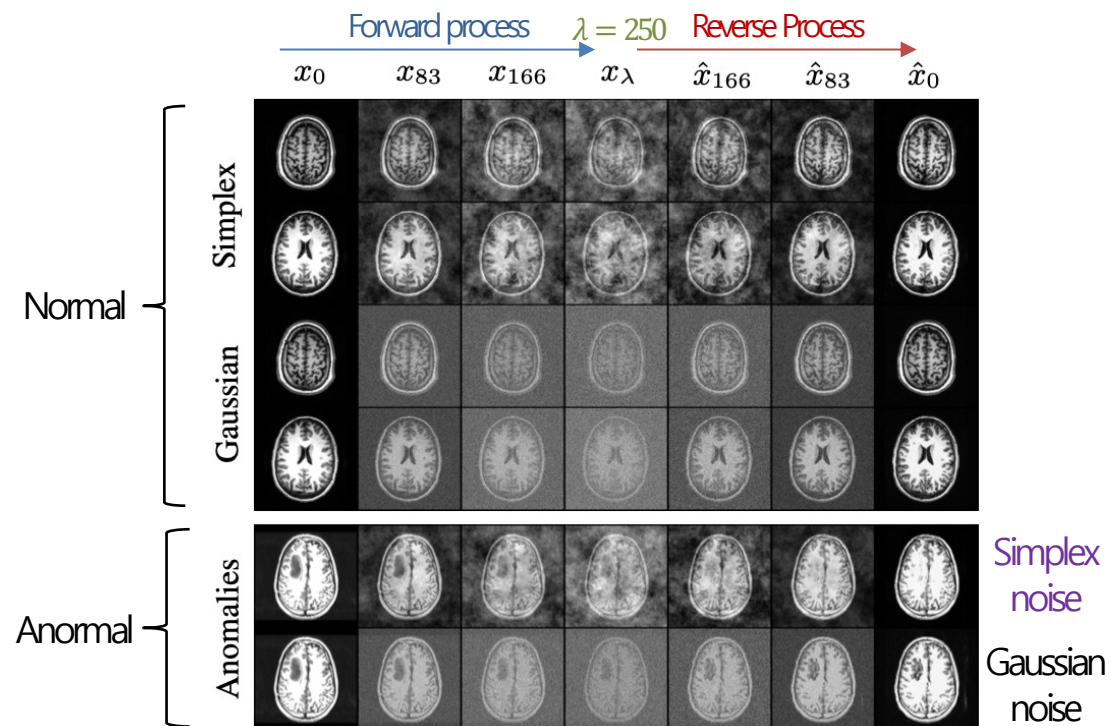
<Text-conditional SDEdit examples>

# Diffusion Models for Anomaly Detection

"AnoDDPM: Anomaly Detection with Denoising Diffusion Probabilistic Models using Simplex Noise", CVPR workshop, 2022

## ❖ AnoDDPM

- A **partial** diffusion anomaly detection
- GAN 기반 모델들에 비해 더 작은 데이터셋을 가지고도 우수한 성능 입증

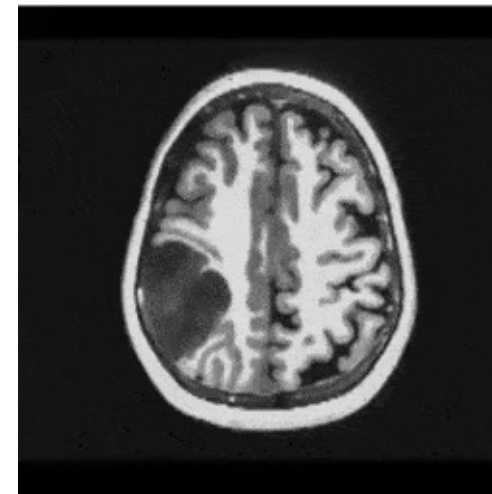
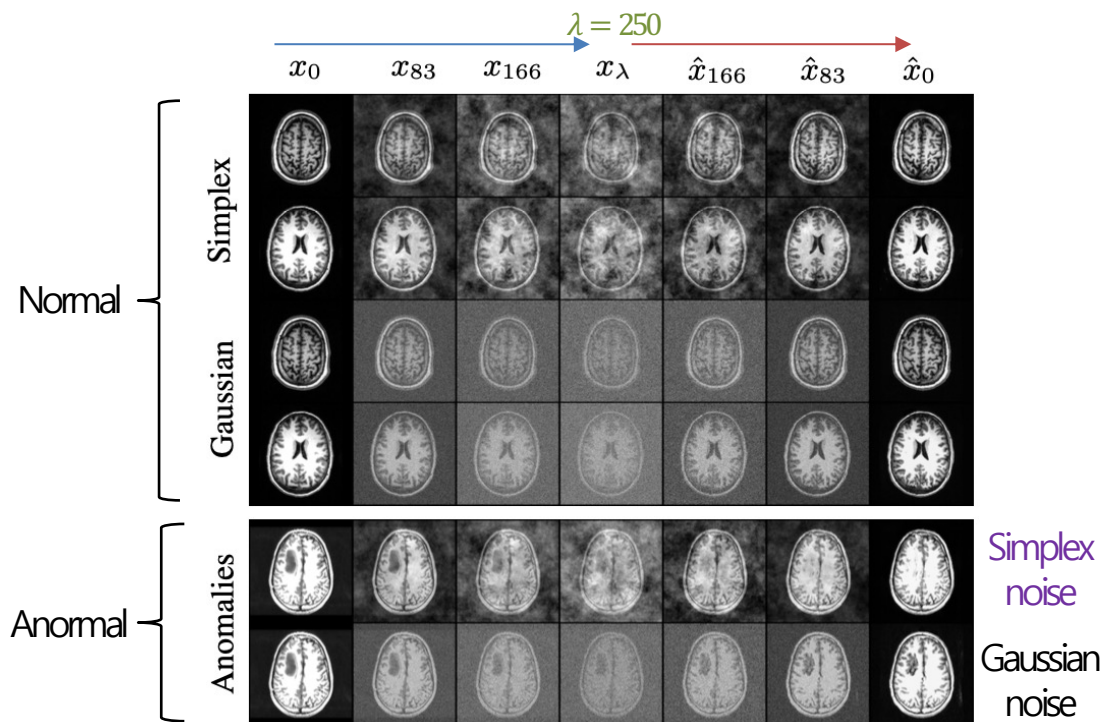


# Diffusion Models for Anomaly Detection

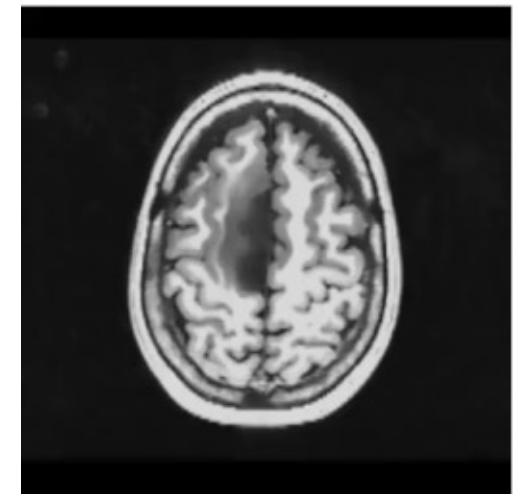
"AnoDDPM: Anomaly Detection with Denoising Diffusion Probabilistic Models using Simplex Noise", CVPR workshop, 2022

## ❖ AnoDDPM

- Gaussian noise을 **multi-scale simplex** noise로 대체



<Gaussian noise>



<Simplex noise>

# Diffusion Models for Anomaly Detection

"AnoDDPM: Anomaly Detection with Denoising Diffusion Probabilistic Models using Simplex Noise", CVPR workshop, 2022

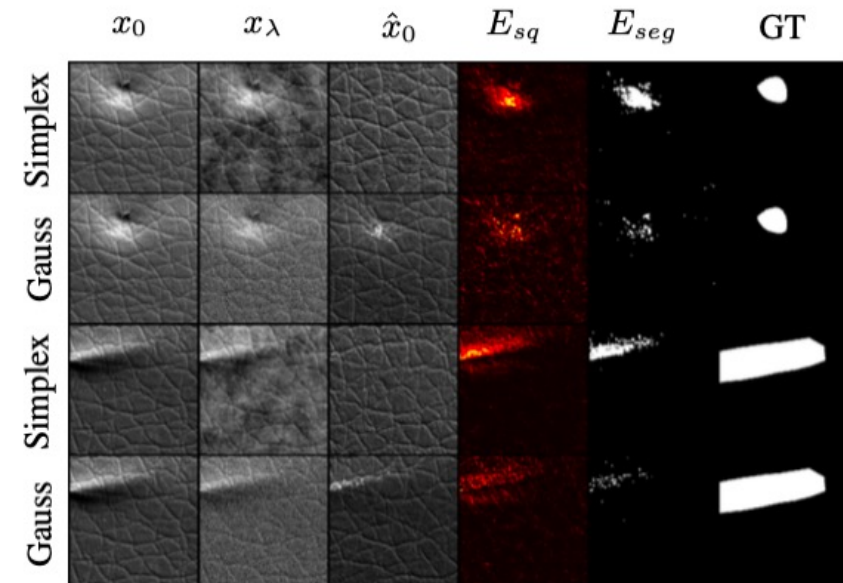
## ❖ Training & Inference

### Algorithm 1 Training

- 1: **repeat**
- 2:  $x_0 \sim q(x_0)$
- 3:  $t \sim \text{Uniform}(\{1, 2, \dots, T - 1, T\})$
- 4: Randomly generate simplex seed
- 5:  $\epsilon \sim \text{Simplex}(\nu = 2^{-6}, N = 6, \gamma = 0.8)$
- 6: Take gradient descent step on:  
 $\nabla_{\theta} [||\epsilon - \epsilon_{\theta}(x_0\sqrt{\bar{\alpha}}_t + \sqrt{1 - \bar{\alpha}}_t\epsilon, t)||^2]$
- 7: **until** converged

### Algorithm 2 Segmentation

- 1:  $x_0 \sim A(x_0)$
- 2:  $x_{\lambda} = x_0\sqrt{\bar{\alpha}}_{\lambda} + \epsilon\sqrt{1 - \bar{\alpha}}_{\lambda}$
- 3: **for**  $t = \lambda, \dots, 1$  **do**
- 4: Randomly generate simplex seed
- 5:  $z \sim \text{Simplex}(2^{-6}, 6, 0.8)$  if  $t > 0$  else  $z = 0$
- 6:  $x_{t-1} = \frac{1}{\sqrt{\alpha}_t}(x_t - \frac{1-\alpha_t}{\sqrt{1-\bar{\alpha}}_t}\epsilon_{\theta}(x_t, t)) + \tilde{\beta}_t z$
- 7: **end for**
- 8:  $E_{sq} = (x_0 - \hat{x}_0)^2$
- 9:  $E_{seg} = E_{sq} > 0.5$
- 10: **return**  $E_{seg}$

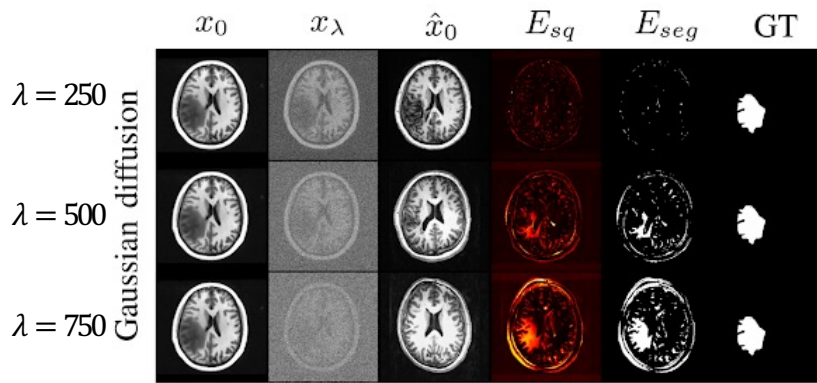




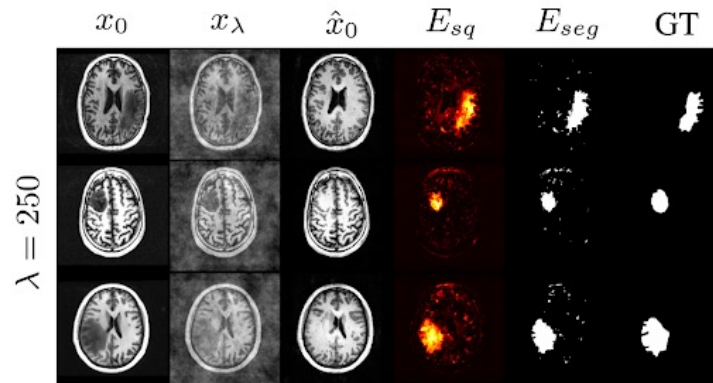
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"AnoDDPM: Anomaly Detection with Denoising Diffusion Probabilistic Models using Simplex Noise", CVPR workshop, 2022

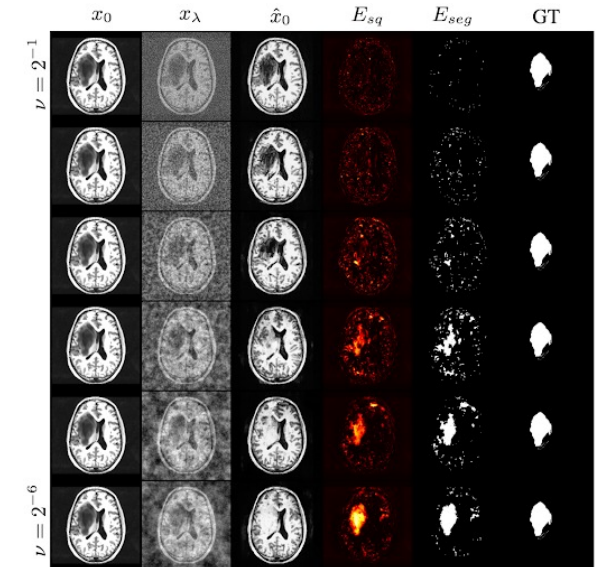
## ❖ Experiments



<Gaussian noise sample>



<Curated simplex noise samples>



<Simplex noise with increasing frequency>

# Diffusion Models for Natural Language Generation

"DiffuSeq: Sequence to Sequence Text Generation with Diffusion Models", ICLR, 2023

## ❖ DiffuSeq

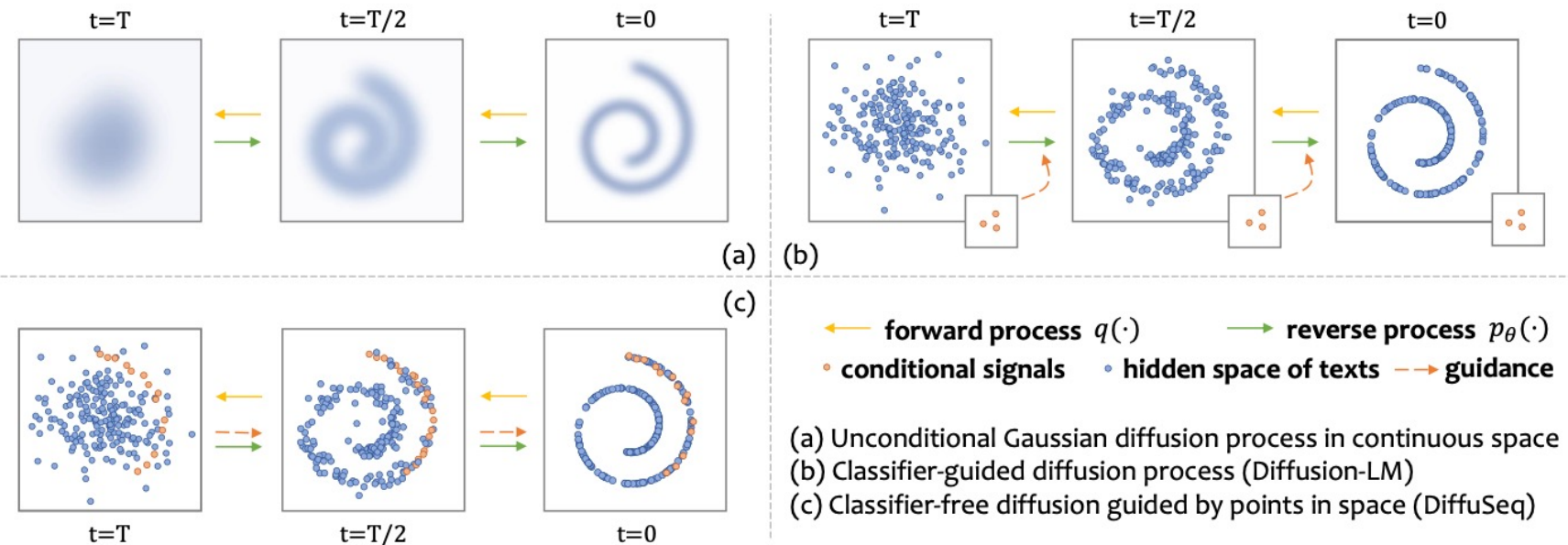
- Discrete한 특성을 지닌 Text에 디퓨전 모델을 적용
- 특히 Sequence-to-Sequence(Seq2Seq) Text Generation에 디퓨전 모델을 최초로 적용

How long was the trip?

It was a year.

E.g. Open-Domain Dialogue

<Sequence to Sequence>



<unconditional, classifier-guided, classifier-free diffusion models>

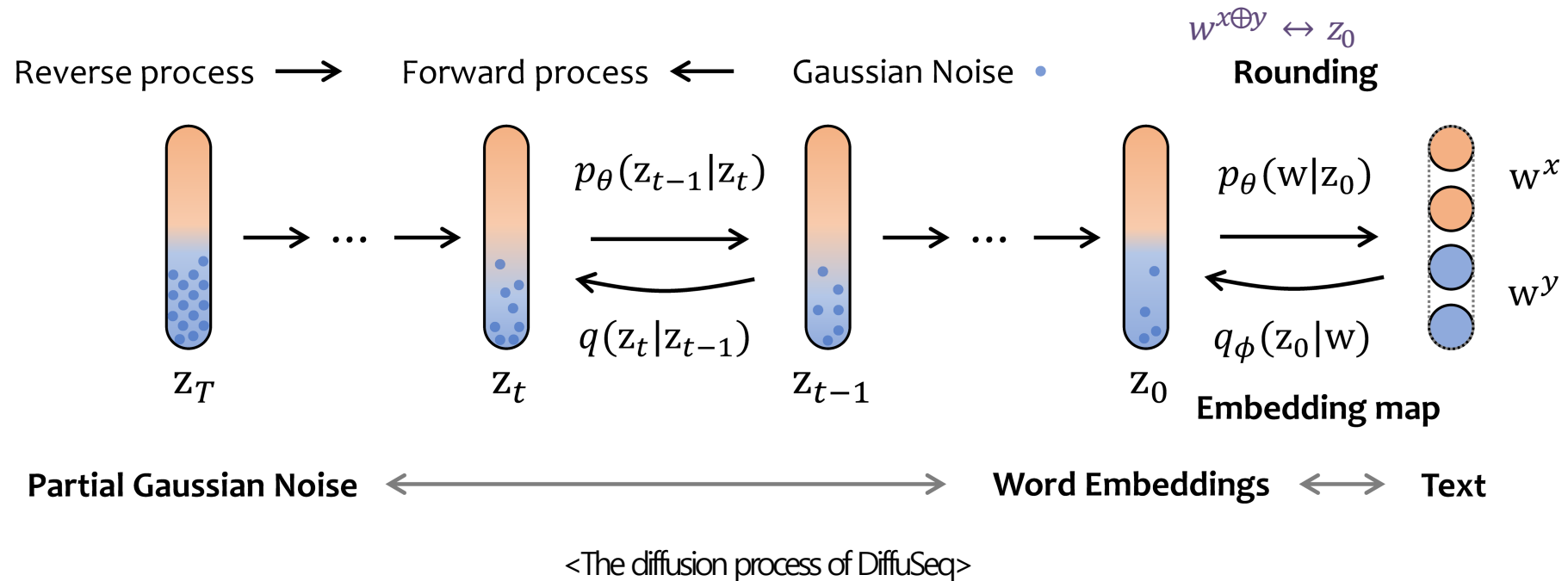


# Diffusion Models for Natural Language Generation

"DiffuSeq: Sequence to Sequence Text Generation with Diffusion Models", ICLR, 2023

## ❖ DiffuSeq

- **Forward process:**  $w^y$ 에 대해서만 noise 부여,  $w^x$ 는 un-noised 상태로 유지
- **Reverse process:** conditional signals  $w^x$ 를 guidance로 활용

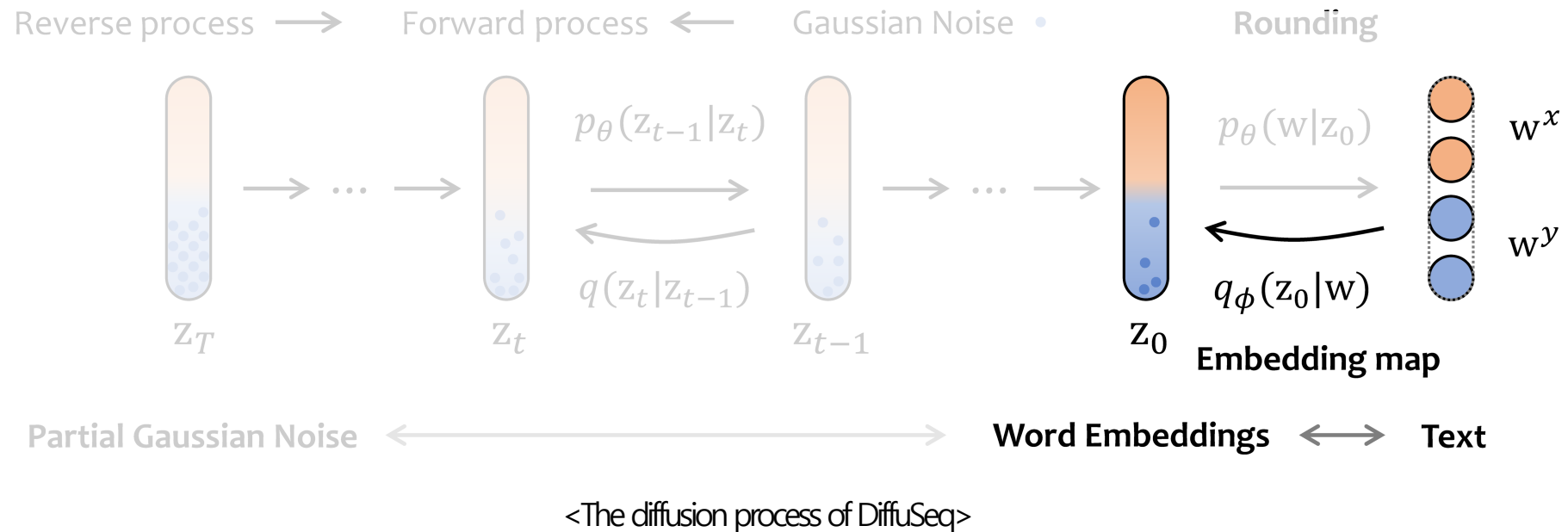


# Diffusion Models for Natural Language Generation

"DiffuSeq: Sequence to Sequence Text Generation with Diffusion Models", ICLR, 2023

## ❖ DiffuSeq

- **Forward process:**  $w^y$ 에 대해서만 noise 부여,  $w^x$ 는 un-noised 상태로 유지
- **Reverse process:** conditional signals  $w^x$ 를 guidance로 활용

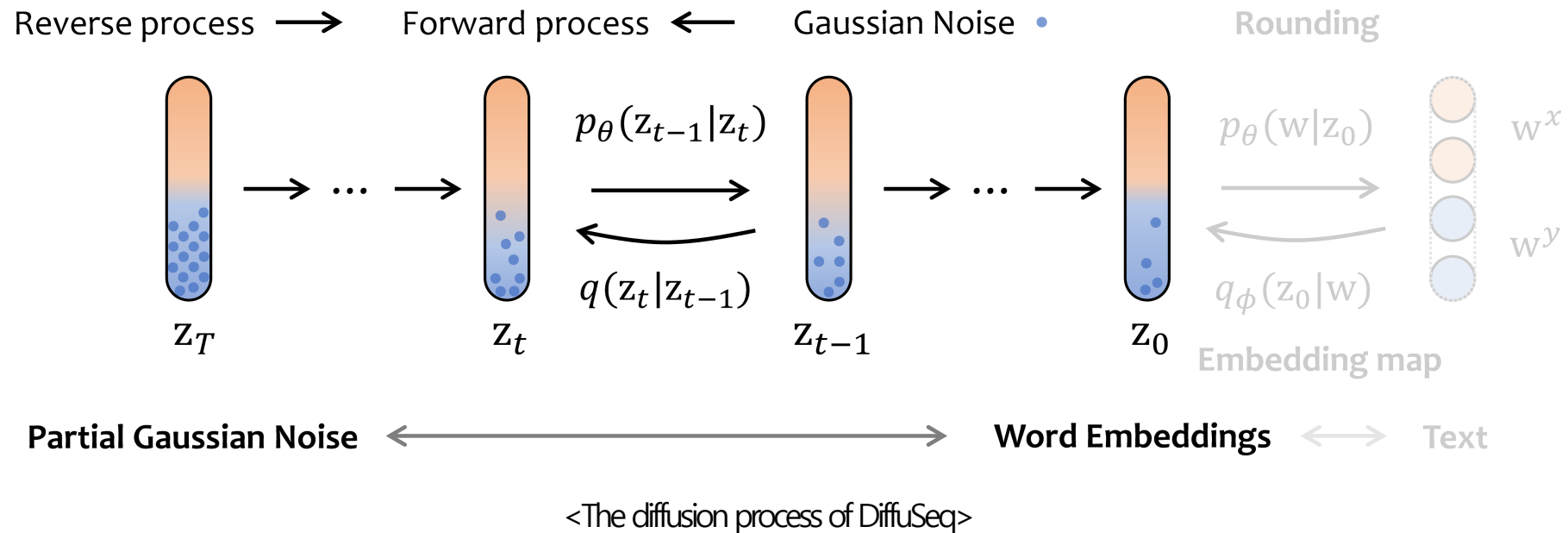


# Diffusion Models for Natural Language Generation

"DiffuSeq: Sequence to Sequence Text Generation with Diffusion Models", ICLR, 2023

## ❖ DiffuSeq

- **Forward process:**  $w^y$ 에 대해서만 noise 부여,  $w^x$ 는 un-noised 상태로 유지 → Partial Noising
- **Reverse process:** conditional signals  $w^x$ 를 guidance로 활용

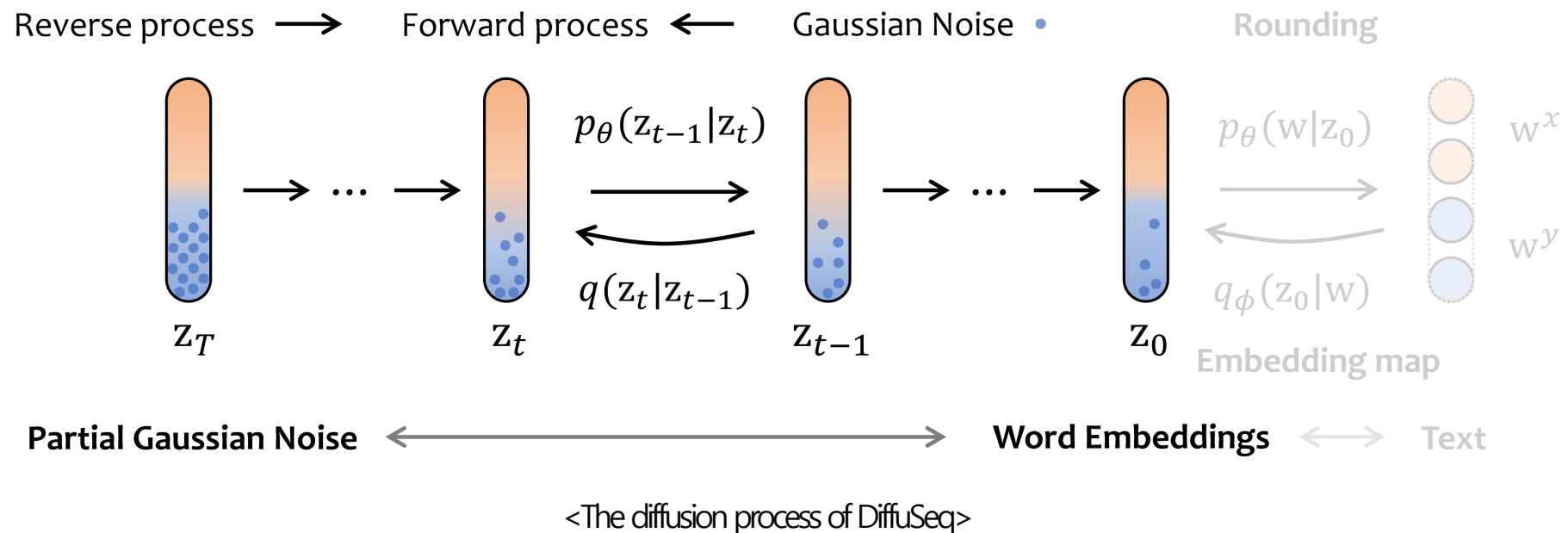


# Diffusion Models for Natural Language Generation

"DiffuSeq: Sequence to Sequence Text Generation with Diffusion Models", ICLR, 2023

## ❖ DiffuSeq

- **Forward process:**  $w^y$ 에 대해서만 noise 부여,  $w^x$ 는 un-noised 상태로 유지
- **Reverse process:** conditional signals  $w^x$ 를 guidance로 활용 → **Partial Denoising**

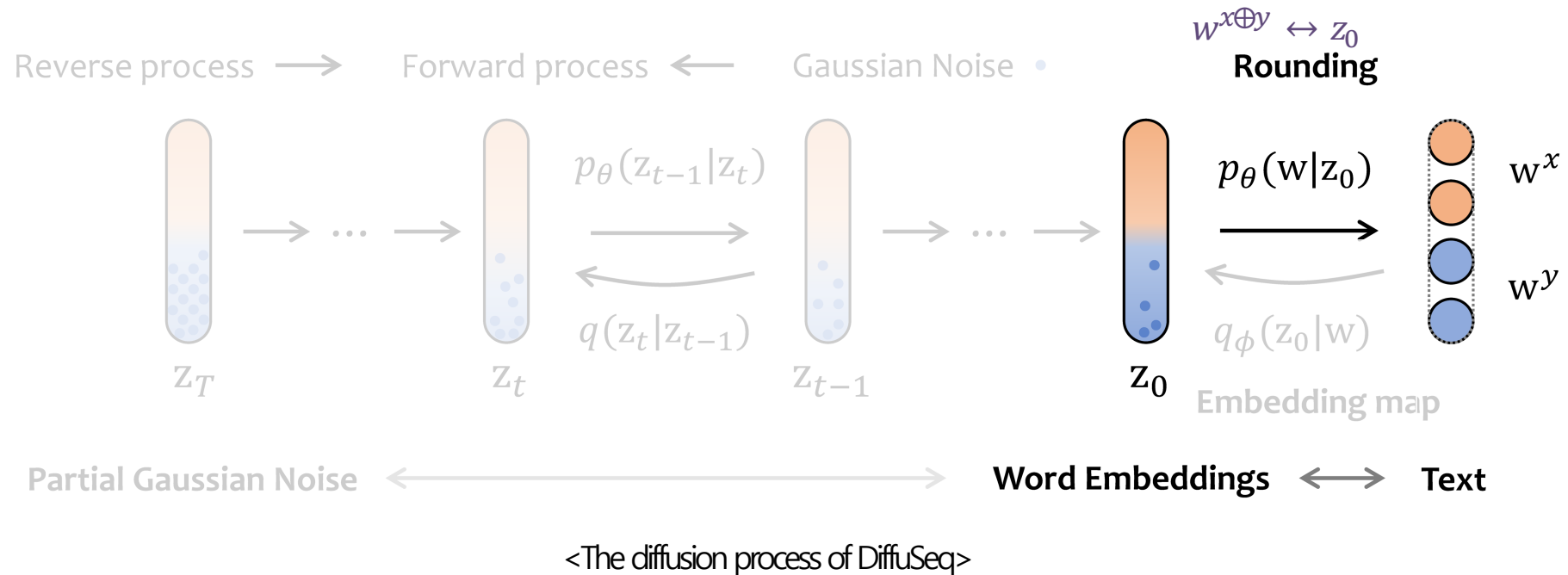


# Diffusion Models for Natural Language Generation

"DiffuSeq: Sequence to Sequence Text Generation with Diffusion Models", ICLR, 2023

## ❖ DiffuSeq

- **Forward process:**  $w^y$ 에 대해서만 noise 부여,  $w^x$ 는 un-noised 상태로 유지
- **Reverse process:** conditional signals  $w^x$ 를 guidance로 활용 → **Partial Denoising**

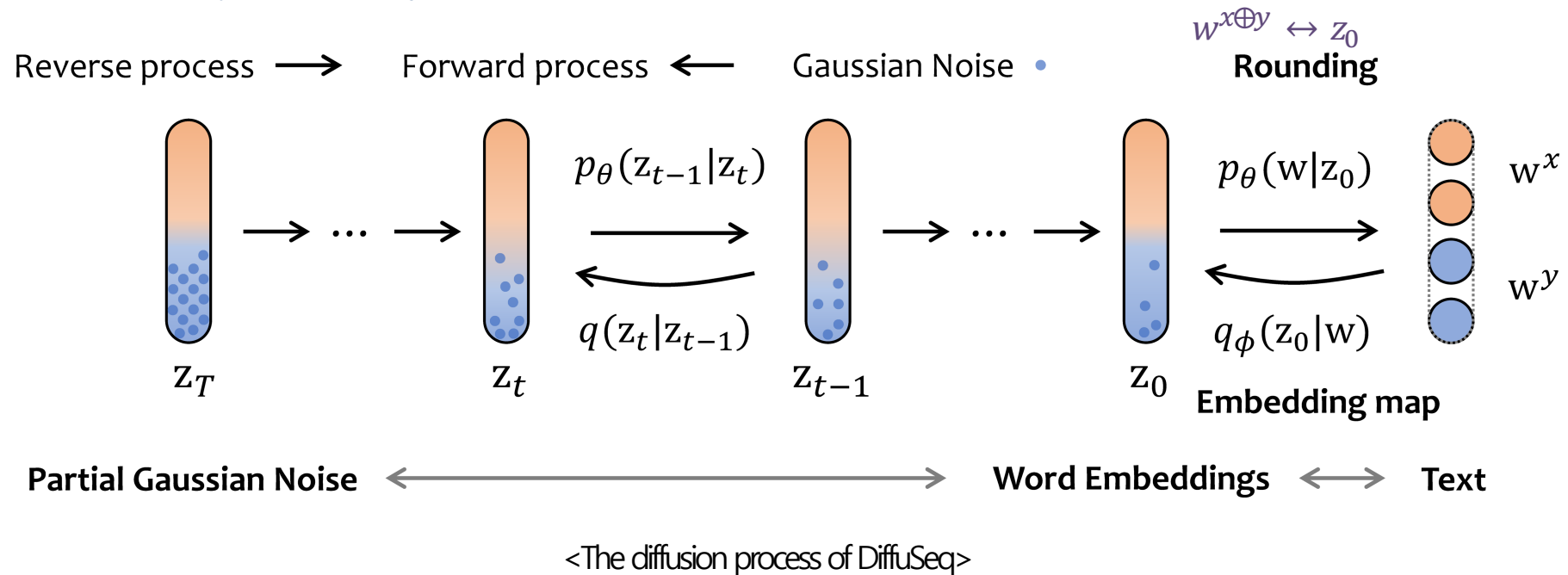


# Diffusion Models for Natural Language Generation

"DiffuSeq: Sequence to Sequence Text Generation with Diffusion Models", ICLR, 2023

## ❖ Training & Inference

- **Training:** Importance sampling을 통해 효율적인 학습 진행
- **Inference:** anchoring operation을 활용
  - 1  $z_t$ 가 임베딩 공간상에 위치하도록
  - 2  $z_{t-1}$ 의 x부분을  $z_0$ 의 x 부분으로 대체



# Diffusion Models for Natural Language Generation

"DiffuSeq: Sequence to Sequence Text Generation with Diffusion Models", ICLR, 2023

## ❖ Experiments

- Sequence-to-Sequence tasks에 대해 우수한 성능을 보임
- 동일한 인풋 시퀀스가 주어졌을 때, 다양한 아웃풋을 생성하는 능력에서 우수함을 보임

Tasks	Methods	BLEU↑	R-L↑	Score↑	dist-1↑	selfB↓ / div-4↑	Len
Open Domain Dialogue	GRU-attention <sup>◇</sup>	0.0068	0.1054	0.4128	0.8998	0.8008/0.1824	4.46
	Transformer-base <sup>◇</sup>	<b>0.0189</b>	0.1039	0.4781	0.7493	0.3698/0.6472	19.5
	GPT2-base FT <sup>•</sup>	0.0108	<b>0.1508</b>	0.5279	0.9194	0.0182/0.9919	16.8
	GPT2-large FT <sup>•</sup>	0.0125	0.1002	<b>0.5293</b>	0.9244	0.0213/0.9938	16.8
	GPVAE-T5 <sup>•</sup>	0.0110	0.1009	0.4317	0.5625	0.3560/0.5551	20.1
	NAR-LevT <sup>‡</sup>	0.0158	0.0550	0.4760	<b>0.9726</b>	0.7103/0.1416	4.11
	DIFFUSEQ (Ours) <sup>‡</sup>	0.0139	<u>0.1056</u>	<u>0.5131</u>	0.9467	<b>0.0144/0.9971</b>	13.6
	GRU-attention <sup>◇</sup>	0.0651	0.2617	0.5222	0.7930	0.9999/0.3178	10.1
	Transformer-base <sup>◇</sup>	0.1663	0.3441	<u>0.6307</u>	<u>0.9309</u>	0.3265/0.7720	10.3
	Question Generation	GPT2-base FT <sup>•</sup>	0.0741	0.2714	0.6052	0.9602	<b>0.1403/0.9216</b>
	GPT2-large FT <sup>•</sup>	0.1110	0.3215	<b>0.6346</b>	<b>0.9670</b>	0.2910/0.8062	9.96
	GPVAE-T5 <sup>•</sup>	0.1251	0.3390	0.6308	0.9381	0.3567/0.7282	11.4
	NAR-LevT <sup>‡</sup>	0.0930	0.2893	0.5491	0.8914	0.9830/0.4776	6.93
	DIFFUSEQ (Ours) <sup>‡</sup>	<b>0.1731</b>	<b>0.3665</b>	0.6123	0.9056	<u>0.2789/0.8103</u>	11.5

Text Simplification	GRU-attention <sup>◇</sup>	0.3256	0.5602	0.7871	0.8883	0.9998/0.3313	18.9
	Transformer-base <sup>◇</sup>	0.2693	0.4907	0.7381	0.8886	0.6924/0.5095	18.5
	GPT2-base FT <sup>•</sup>	0.3083	0.5461	0.8021	0.9439	0.5444/0.6047	16.1
	GPT2-large FT <sup>•</sup>	0.2693	0.5111	0.7882	0.9464	0.6042/0.5876	15.4
	GPVAE-T5 <sup>•</sup>	0.3392	0.5828	<b>0.8166</b>	0.9308	0.8147/0.4355	18.5
	NAR-LevT <sup>‡</sup>	0.2052	0.4402	0.7254	<b>0.9715</b>	0.9907/0.3271	8.31
	DIFFUSEQ (Ours) <sup>‡</sup>	<b>0.3622</b>	<b>0.5849</b>	<u>0.8126</u>	<u>0.9264</u>	<b>0.4642/0.6604</b>	17.7
	GRU-attention <sup>◇</sup>	0.1894	0.5129	0.7763	0.9423	0.9958/0.3287	8.30
	Transformer-base <sup>◇</sup>	<b>0.2722</b>	0.5748	<u>0.8381</u>	0.9748	0.4483/0.7345	11.2
	Paraphrase	GPT2-base FT <sup>•</sup>	0.1980	0.5212	0.8246	0.9798	0.5480/0.6245
	GPT2-large FT <sup>•</sup>	0.2059	0.5415	0.8363	<b>0.9819</b>	0.7325/0.5020	9.53
	GPVAE-T5 <sup>•</sup>	0.2409	<b>0.5886</b>	<b>0.8466</b>	0.9688	0.5604/0.6169	9.60
	NAR-LevT <sup>‡</sup>	0.2268	0.5795	0.8344	0.9790	0.9995/0.3329	8.85
	DIFFUSEQ (Ours) <sup>‡</sup>	0.2413	<u>0.5880</u>	<u>0.8365</u>	<u>0.9807</u>	<b>0.2732/0.8641</b>	11.2

# Diffusion Models for Natural Language Generation

"DiffuSeq: Sequence to Sequence Text Generation with Diffusion Models", ICLR, 2023

## ❖ Experiments

- Sequence-to-Sequence tasks에 대해 우수한 성능을 보임
- 동일한 인풋 시퀀스가 주어졌을 때, 다양한 아웃풋을 생성하는 능력에서 우수함을 보임

<i>Original sentence: How do I make friends.</i>		<i>Paraphrase reference: How to make friends ?</i>
<b>GPT2-large finetune</b>	<b>GPVAE-T5</b>	<b>DIFFUSEQ</b>
How can I make friends?	How can I make friends?	How can I make friends better?
How can I make friends?	How do I make friends?	How can I make friends?
How can I make friends?	How can I make friends?	How do you make friends?
How can I make friends?	How can I make friends?	What is the best way to make friends?
How do I make friends and keep them?	What's the best way to make friends and make make friends?	How can I make friends and more something?



# Diffusion Models for Time-series Forecasting

"Autoregressive denoising diffusion models for multivariate probabilistic time series forecasting", ICML, 2021

## ❖ TimeGrad

- 다변량 시계열 예측을 위한 **autoregressive** denoising diffusion model

Data

$$x_1, x_2, \dots, x_{t_0-1}, x_{t_0}, \dots, x_{T-1}, x_T \in R^D$$

└──────────────────┘
└──────────────────┘  
Past
Future

Conditional distribution

$$q_x(x_{t_0:T}^0 | x_{1:t_0-1}^0, \overset{\text{covariate}}{c_{1:T}}) = \prod_{t=t_0}^T q_x(x_t^0 | x_{1:t-1}^0, c_{1:T})$$

$$q_x(x_{t_0:T}^0 | x_{1:t_0-1}^0)$$

=

$$q_x(x_{t_0}^0 | x_{1:t_0-1}^0)$$

×

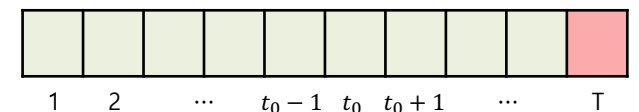
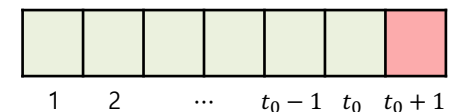
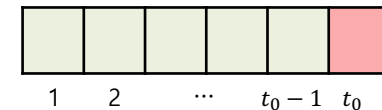
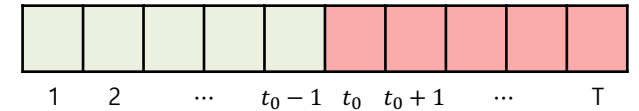
$$q_x(x_{t_0}^0 | x_{1:t_0-1}^0)$$

×

⋮

×

$$q_x(x_T^0 | x_{1:T-1}^0)$$



# Diffusion Models for Time-series Forecasting

"Autoregressive denoising diffusion models for multivariate probabilistic time series forecasting", ICML, 2021

## ❖ TimeGrad

- 다변량 시계열 예측을 위한 autoregressive denoising diffusion model

Data

$$x_1, x_2, \dots, x_{t_0-1}, x_{t_0}, \dots, x_{T-1}, x_T \in R^D$$

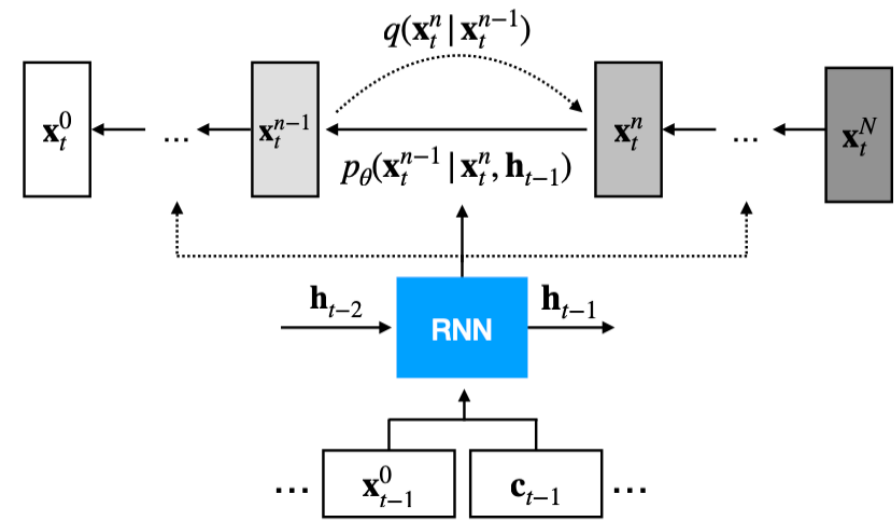
Past
Future

Conditional distribution

$$q_x(x_{t_0:T}^0 | x_{1:t_0-1}^0, c_{1:T}) = \prod_{t=t_0}^T q_x(x_t^0 | x_{1:t-1}^0, c_{1:T})$$

covariate

$$\rightarrow \prod_{t=t_0}^T p_\theta(x_t^0 | h_{t-1})$$



$$h_t = \text{RNN}_\theta(\text{concat}(x_t^0, c_t), h_{t-1})$$

# Diffusion Models for Time-series Forecasting

"Autoregressive denoising diffusion models for multivariate probabilistic time series forecasting", ICML, 2021

## ❖ Training & sampling

Data

$$x_1, x_2, \dots, x_{t_0-1}, x_{t_0}, \dots, x_{T-1}, x_T \in R^D$$

└──────────────────┘
└──────────────────┘  
Past
Future

Conditional distribution

$$q_x(x_{t_0:T}^0 | x_{1:t_0-1}^0, c_{1:T}) = \prod_{t=t_0}^T q_x(x_t^0 | x_{1:t-1}^0, c_{1:T})$$

covariate

$$\rightarrow \prod_{t=t_0}^T p_\theta(x_t^0 | h_{t-1})$$

---

**Algorithm 1** Training for each time series step  $t \in [t_0, T]$

---

**Input:** data  $\mathbf{x}_t^0 \sim q_x(\mathbf{x}_t^0)$  and state  $\mathbf{h}_{t-1}$

**repeat**

Initialize  $n \sim \text{Uniform}(1, \dots, N)$  and  $\epsilon \sim \mathcal{N}(\mathbf{0}, \mathbf{I})$

Take gradient step on

$$\nabla_\theta \|\epsilon - \epsilon_\theta(\sqrt{\bar{\alpha}_n} \mathbf{x}_t^0 + \sqrt{1 - \bar{\alpha}_n} \epsilon, \mathbf{h}_{t-1}, n)\|^2$$

**until** converged

---



---

**Algorithm 2** Sampling  $\mathbf{x}_t^0$  via annealed Langevin dynamics

---

**Input:** noise  $\mathbf{x}_t^N \sim \mathcal{N}(\mathbf{0}, \mathbf{I})$  and state  $\mathbf{h}_{t-1}$

**for**  $n = N$  **to** 1 **do**

**if**  $n > 1$  **then**

$\mathbf{z} \sim \mathcal{N}(\mathbf{0}, \mathbf{I})$

**else**

$\mathbf{z} = \mathbf{0}$

**end if**

$\mathbf{x}_t^{n-1} = \frac{1}{\sqrt{\alpha_n}} (\mathbf{x}_t^n - \frac{\beta_n}{\sqrt{1-\alpha_n}} \epsilon_\theta(\mathbf{x}_t^n, \mathbf{h}_{t-1}, n)) + \sqrt{\Sigma_\theta} \mathbf{z}$

**end for**

**Return:**  $\mathbf{x}_t^0$

---

# Diffusion Models for Time-series Forecasting

"Autoregressive denoising diffusion models for multivariate probabilistic time series forecasting", ICML, 2021

## ❖ Experiments

Table 2. Test set CRPS<sub>sum</sub> comparison (lower is better) of models on six real world data sets. Mean and standard error metrics for TimeGrad obtained by re-training and evaluating 10 times.

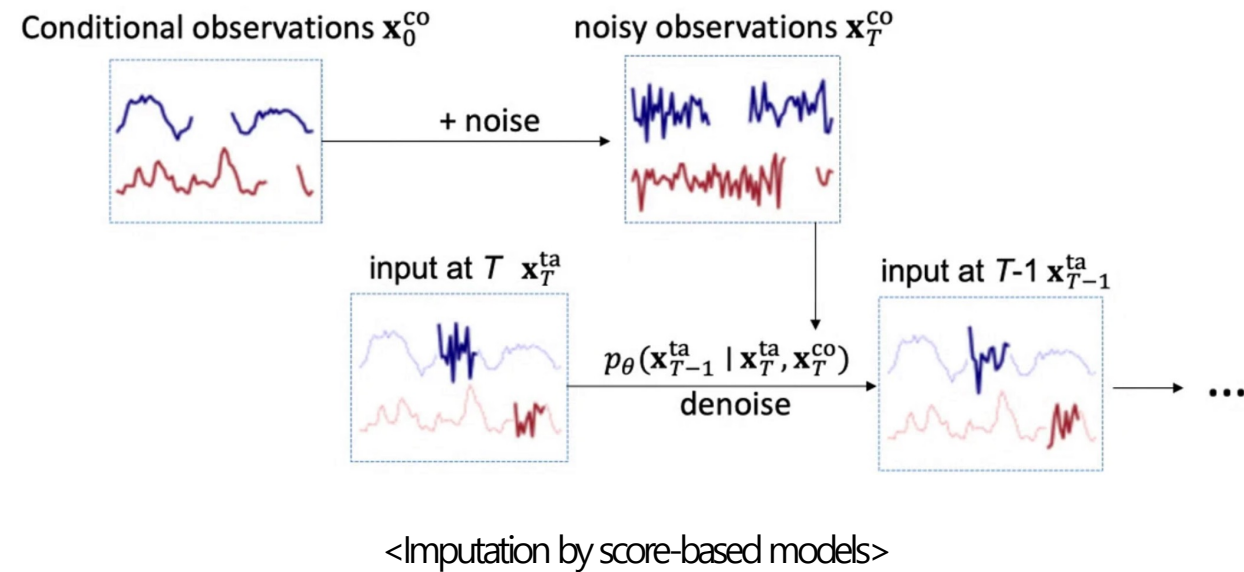
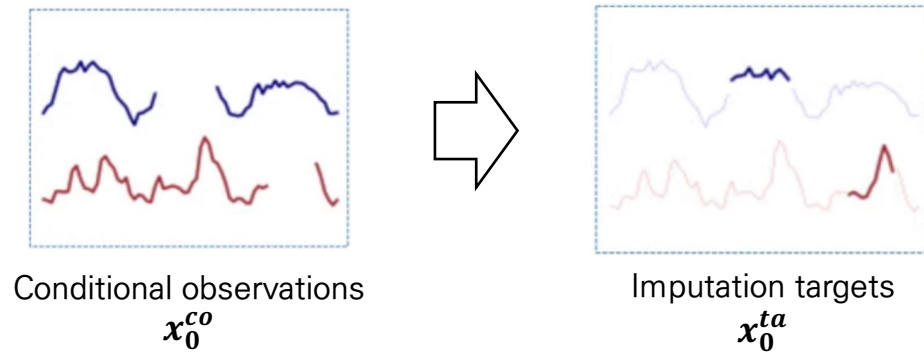
Method	Exchange	Solar	Electricity	Traffic	Taxi	Wikipedia
VES	<b>0.005</b> ±0.000	0.9±0.003	0.88±0.0035	0.35±0.0023	-	-
VAR	<b>0.005</b> ±0.000	0.83±0.006	0.039±0.0005	0.29±0.005	-	-
VAR-Lasso	0.012±0.0002	0.51±0.006	0.025±0.0002	0.15±0.002	-	3.1±0.004
GARCH	0.023±0.000	0.88±0.002	0.19±0.001	0.37±0.0016	-	-
KVAE	0.014±0.002	0.34±0.025	0.051±0.019	0.1±0.005	-	0.095±0.012
Vec-LSTM ind-scaling	0.008±0.001	0.391±0.017	0.025±0.001	0.087±0.041	0.506±0.005	0.133±0.002
Vec-LSTM lowrank-Copula	0.007±0.000	0.319±0.011	0.064±0.008	0.103±0.006	0.326±0.007	0.241±0.033
GP scaling	0.009±0.000	0.368±0.012	0.022±0.000	0.079±0.000	0.183±0.395	1.483±1.034
GP Copula	0.007±0.000	0.337±0.024	0.0245±0.002	0.078±0.002	0.208±0.183	0.086±0.004
Transformer MAF	<b>0.005</b> ±0.003	0.301±0.014	0.0207±0.000	0.056±0.001	0.179±0.002	0.063±0.003
<b>TimeGrad</b>	0.006±0.001	<b>0.287</b> ±0.02	<b>0.0206</b> ±0.001	<b>0.044</b> ±0.006	<b>0.114</b> ±0.02	<b>0.0485</b> ±0.002

# Diffusion Models for Time-series Imputation

"CSDI: Conditional Score-based Diffusion Models for Probabilistic Time Series Imputation", NeurIPS, 2021

## ❖ CSDI

- **확률적 시계열 imputation을 위한** Conditional Score-based Diffusion Model
- Imputation task :  $x_0^{co} \rightarrow x_0^{ta}$

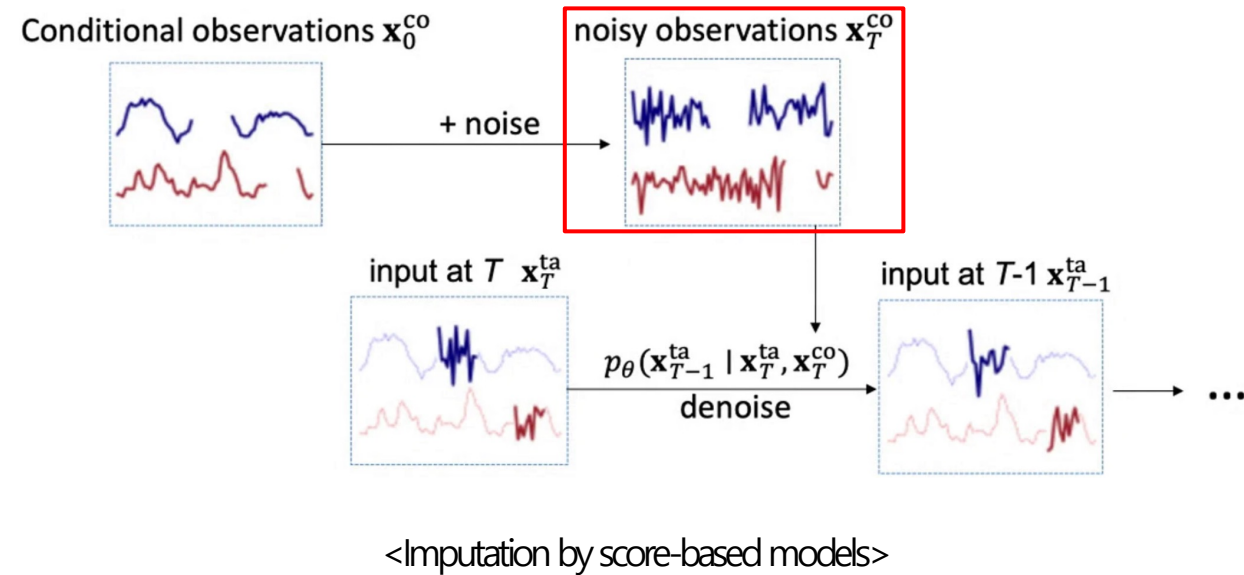
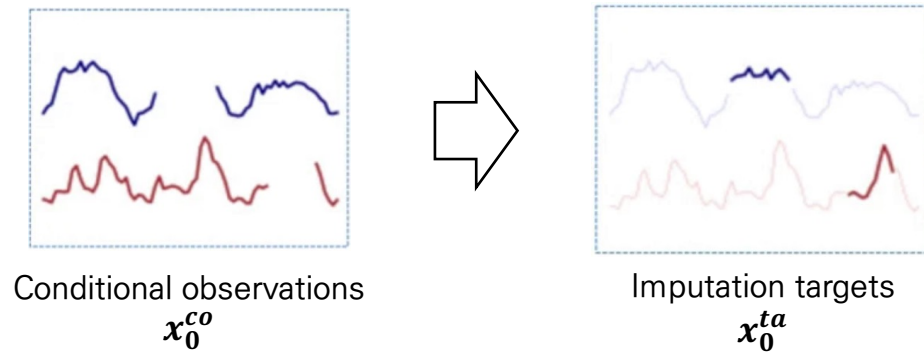


# Diffusion Models for Time-series Imputation

"CSDI: Conditional Score-based Diffusion Models for Probabilistic Time Series Imputation", NeurIPS, 2021

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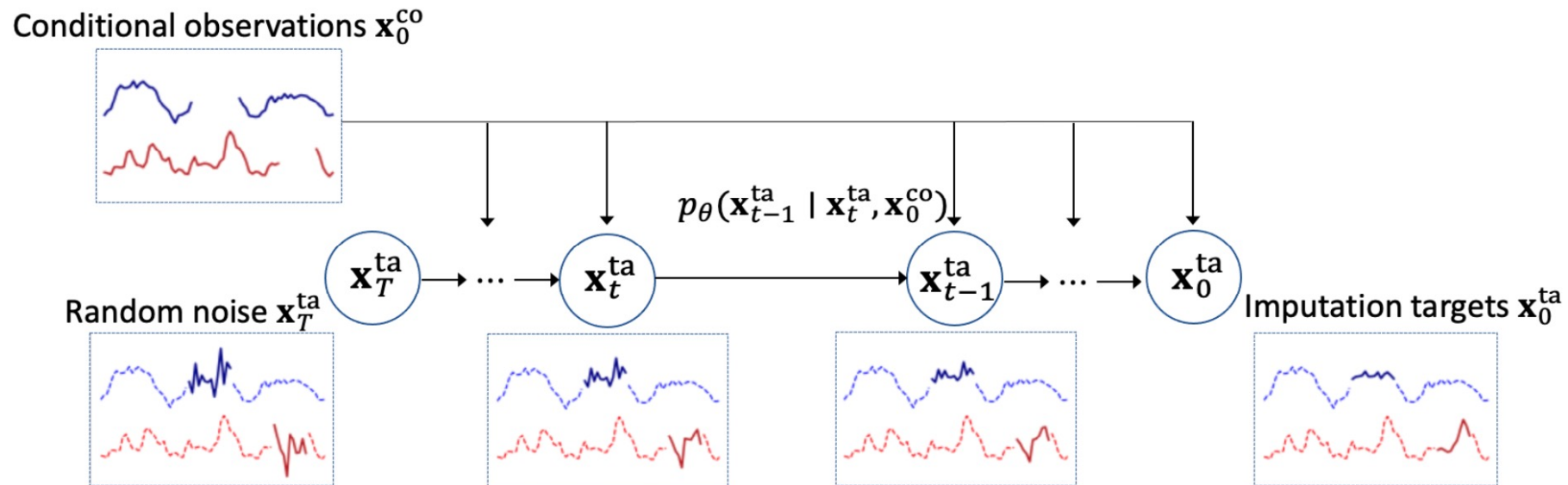


# Diffusion Models for Time-series Imputation

"CSDI: Conditional Score-based Diffusion Models for Probabilistic Time Series Imputation", NeurIPS, 2021

## ❖ CSDI

- 관측치를 reverse process의 **conditional input**으로 활용

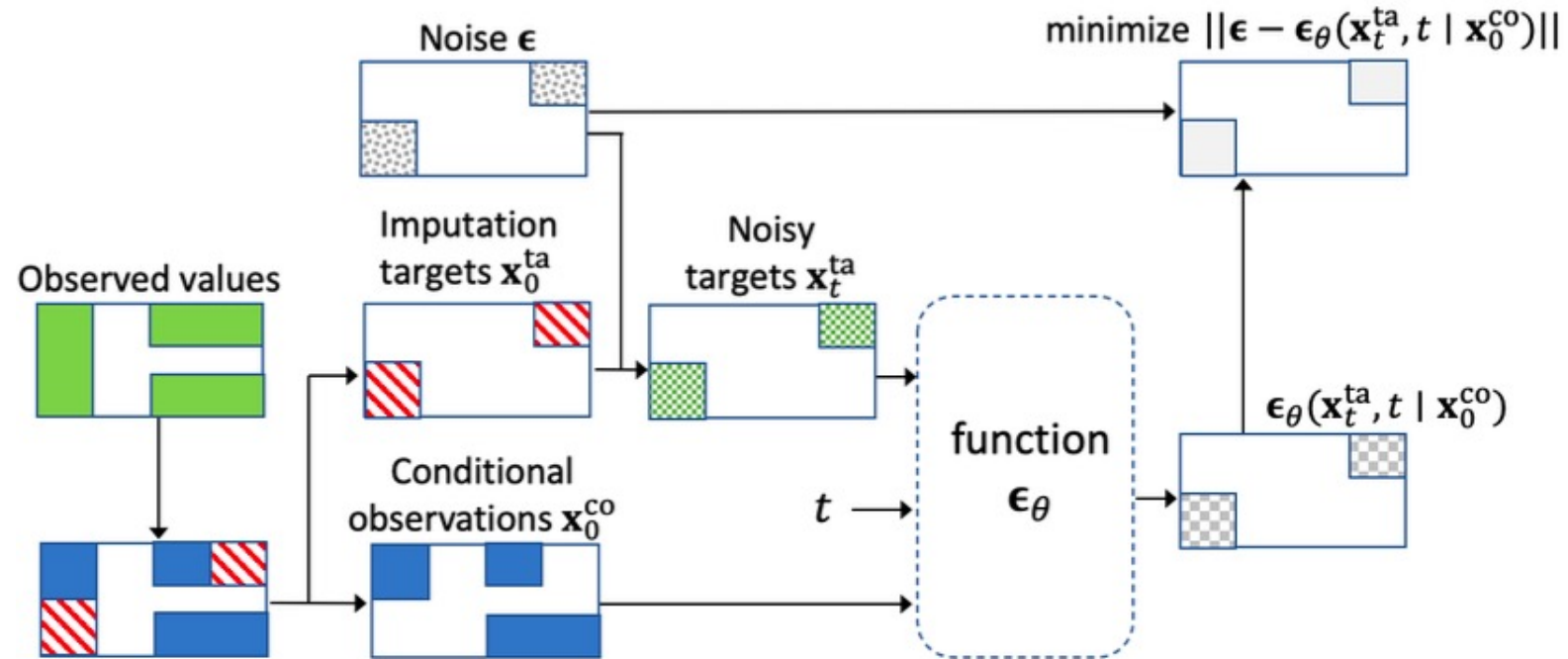


# Diffusion Models for Time-series Imputation

"CSDI: Conditional Score-based Diffusion Models for Probabilistic Time Series Imputation", NeurIPS, 2021

## ❖ Training

- Masked language modeling에서 착안하여 **self-supervised training method** 적용



<The self-supervised training procedure of CSDI>

- (1) Random strategy
- (2) Historical strategy
- (3) Mix strategy
- (4) Test pattern strategy



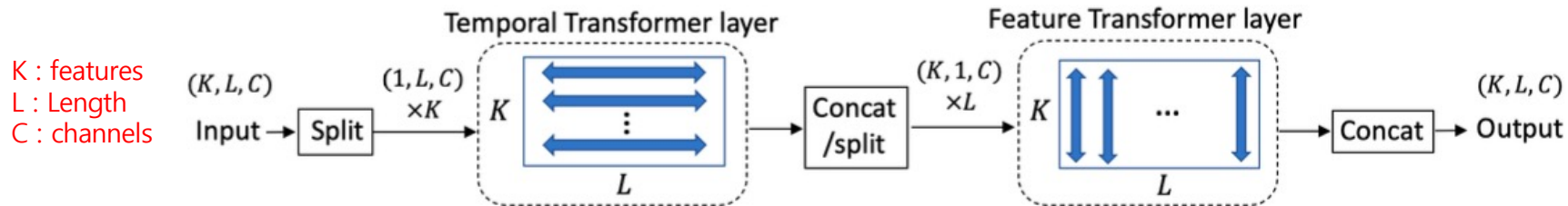
# Diffusion Models for Time-series Imputation

"CSDI: Conditional Score-based Diffusion Models for Probabilistic Time Series Imputation", NeurIPS, 2021

❖  $x_0^{co}$  &  $x_0^{ta}$  at training and sampling

	imputation targets $x_0^{ta}$	conditional observations $x_0^{co}$
sampling (imputation)	all missing values	all observed values
training	a subset of the observed values (sampled by a target choice strategy)	the remaining observed values

❖ 2D attention mechanism



# Diffusion Models for Time-series Imputation

"CSDI: Conditional Score-based Diffusion Models for Probabilistic Time Series Imputation", NeurIPS, 2021

## ❖ Experiments

Table 2: Comparing CRPS for **probabilistic imputation** baselines and CSDI (lower is better). We report the mean and the standard error of CRPS for five trials.

	healthcare			air quality
	10% missing	50% missing	90% missing	
Multitask GP [31]	0.489(0.005)	0.581(0.003)	0.942(0.010)	0.301(0.003)
GP-VAE [10]	0.574(0.003)	0.774(0.004)	0.998(0.001)	0.397(0.009)
V-RIN [32]	0.808(0.008)	0.831(0.005)	0.922(0.003)	0.526(0.025)
unconditional	0.360(0.007)	0.458(0.008)	0.671(0.007)	0.135(0.001)
<b>CSDI (proposed)</b>	<b>0.238(0.001)</b>	<b>0.330(0.002)</b>	<b>0.522(0.002)</b>	<b>0.108(0.001)</b>

Table 3: Comparing MAE for **deterministic imputation** methods and CSDI. We report the mean and the standard error for five trials. The asterisks mean the results of the method are cited from the original paper.

	healthcare			air quality
	10% missing	50% missing	90% missing	
V-RIN [32]	0.271(0.001)	0.365(0.002)	0.606(0.006)	25.4(0.62)
BRITS [7]	0.284(0.001)	0.368(0.002)	0.517(0.002)	14.11(0.26)
BRITS [7] (*)	0.278	—	—	11.56
GLIMA [21] (*)	0.265	—	—	10.54
RDIS [20]	0.319(0.002)	0.419(0.002)	0.631(0.002)	22.11(0.35)
unconditional	0.326(0.008)	0.417(0.010)	0.625(0.010)	12.13(0.07)
<b>CSDI (proposed)</b>	<b>0.217(0.001)</b>	<b>0.301(0.002)</b>	<b>0.481(0.003)</b>	<b>9.60(0.04)</b>

# Diffusion Models for Time-series Imputation

"CSDI: Conditional Score-based Diffusion Models for Probabilistic Time Series Imputation", NeurIPS, 2021

## ❖ Experiments

Table 4: Comparing the state-of-the-art **interpolation** methods with CSDI for the healthcare dataset. We report the mean and the standard error of CRPS for five trials.

	10% missing	50% missing	90% missing
Latent ODE [35]	0.700(0.002)	0.676(0.003)	0.761(0.010)
mTANs [22]	0.526(0.004)	0.567(0.003)	0.689(0.015)
<b>CSDI (proposed)</b>	<b>0.380(0.002)</b>	<b>0.418(0.001)</b>	<b>0.556(0.003)</b>

Table 5: Comparing **probabilistic forecasting** methods with CSDI. We report the mean and the standard error of CRPS-sum for three trials. The baseline results are cited from the original paper. 'TransMAF' is the abbreviation for 'Transformer MAF'.

	solar	electricity	traffic	taxi	wiki
GP-copula [34]	0.337(0.024)	0.024(0.002)	0.078(0.002)	0.208(0.183)	0.086(0.004)
TransMAF [36]	0.301(0.014)	0.021(0.000)	0.056(0.001)	0.179(0.002)	0.063(0.003)
TLAE [37]	<b>0.124(0.033)</b>	0.040(0.002)	0.069(0.001)	0.130(0.006)	0.241(0.001)
TimeGrad [25]	0.287(0.020)	0.021(0.001)	0.044(0.006)	<b>0.114(0.020)</b>	0.049(0.002)
<b>CSDI (proposed)</b>	0.298(0.004)	<b>0.017(0.000)</b>	<b>0.020(0.001)</b>	0.123(0.003)	<b>0.047(0.003)</b>

# Conclusion

## Applications of Diffusion Models

### ❖ Applications of Diffusion Models

- **Text-to-Image Generation**

- ✓ **GLIDE**: Classifier-free guidance와 CLIP guidance를 통해 text-guided image generation and Editing 수행

- **Anomaly Detection**

- ✓ **AnoDDPM**: A partial diffusion anomaly detection with Gaussian noise and multi-scale simplex noise

- **Natural Language Generation**

- ✓ **DiffuSeq**: Sequence to Sequence Text Generation with Diffusion Models in classifier-free manner

- **Time-series Forecasting & Imputation**

- ✓ **TimeGrad**: Autoregressive denoising diffusion models for multivariate probabilistic time series forecasting
- ✓ **CSDI**: Conditional Score-based Diffusion Models for Probabilistic Time Series Imputation